

**MATH 473**  
**WINTER 2019**  
**HOMEWORK 36**

1. Let  $G$  be a finite group acting transitively on a set  $\Omega$  of size greater than 1. Prove that there is some  $g \in G$  such that  $|\text{fix}_\Omega(G)| = 0$ .
2. Determine the number of ways to color the faces of a tetrahedron with  $n$  colors (up to symmetry).
3. Prove that the symmetry group of the cube is isomorphic to  $S_4$ .
4. Determine the number of ways to color the faces of a cube with  $n$  colors (up to symmetry).